There are eight (8) problems in this packet. Each team member should have a copy of the problems. These problems are NOT necessarily sorted by difficulty. You may solve them in any order.

Remember input/output for the contest will be from stdin to stdout. stderr will be ignored. Do not refer to or use external files in your source code. Extra white space at the end of lines is ignored, but extra white space at the beginning or within text on a line is not ignored. An extra blank line of output is ignored, but blank lines at the beginning or between lines of text are not ignored.

Have Fun & Good Luck! 😊

Problem 1. The Chinese Zodiac

Problem 2. Elo Rating Equation

Problem 3. Spiral of Theodorus

Problem 4. Lily’s Birthday Party

Problem 5. Vigenère’s Cipher

Problem 6. Medfield GPA Calculator

Problem 7. Australia Word Search

Problem 8. Windows
Problem 1
The Chinese Zodiac

The Chinese Zodiac is a scheme that relates each year to an animal and its reputed attributes, according to a 12-year cycle. It is divided into 12 parts, and each part is associated with names of animals. The twelve animals are also linked to the traditional Chinese agricultural calendar, which runs alongside the better known lunar calendar. 2010 is the year of the tiger, and those born in this year are said to be unpredictable, rebellious, daring, impulsive, and generous.

Your job is to write a program that converts a given year to its corresponding animal in the Chinese Zodiac. Below is a table starting in the year 1965 along with its corresponding animal. 1965 was the year of the snake, and so were 1977, 1989, and 2001 given the 12-year cycle.

<table>
<thead>
<tr>
<th>Year</th>
<th>Animal</th>
</tr>
</thead>
<tbody>
<tr>
<td>1965</td>
<td>snake</td>
</tr>
<tr>
<td>1966</td>
<td>horse</td>
</tr>
<tr>
<td>1967</td>
<td>sheep</td>
</tr>
<tr>
<td>1968</td>
<td>monkey</td>
</tr>
<tr>
<td>1969</td>
<td>rooster</td>
</tr>
<tr>
<td>1970</td>
<td>dog</td>
</tr>
<tr>
<td>1971</td>
<td>pig</td>
</tr>
<tr>
<td>1972</td>
<td>rat</td>
</tr>
<tr>
<td>1973</td>
<td>ox</td>
</tr>
<tr>
<td>1974</td>
<td>tiger</td>
</tr>
<tr>
<td>1975</td>
<td>rabbit</td>
</tr>
<tr>
<td>1976</td>
<td>dragon</td>
</tr>
</tbody>
</table>

Input
The first line of input contains an integer \( T \), \( 1 \leq T \leq 1000 \), which is the number of test cases. The next \( T \) lines will each contain a valid four digit year in the range from 1965 through 2165.

Output
There will be \( T \) lines of output, one per year. The general format of an output line is as follows.
<year input> is the year of the <corresponding animal>

Sample Input
4
1981
1970
2165
2011

Output Corresponding to Sample Input
1981 is the year of the rooster
1970 is the year of the dog
2165 is the year of the ox
2011 is the year of the rabbit
Problem 2

Elo Rating Equation

The Social Network is a popular new movie describing the story of the founders of the social-networking website, Facebook. For those of you who have seen the movie, you may remember Mark Zuckerberg inviting his friend Eduardo to give him his chess algorithm at the beginning of the movie when Mark creates Facemash.com. You may also remember he scribbles something like this on the window of his Harvard dorm room:

\[
\frac{(\text{Total of opponents' ratings} + 400 \times (\text{Wins} - \text{Losses}))}{\text{(Total Games)}}
\]

This is a variation of what is known as the Elo Rating Equation, and is a simple way to get an estimate of a PR (Performance Rating). In today’s society, the Elo Rating system is an algorithm used by many ranking systems to predict the outcome of matches, and ensure a level of fairness between teams of different levels playing against each other. FIFA even uses the Elo rating system to rank soccer teams. Your job is to write a computer program that applies it to the top college football teams of a given season after at least seven games are played.

Input & Output
The first line of input contains an integer \( T \), \((1 \leq T \leq 1000)\), which is the number of teams. The next \( T \) lines will contain team records, one line for each team. Each team record starts with the name of a team (a single string with no spaces), followed by a space, and the teams total wins and losses in the format wins-losses where wins and losses are both nonnegative integers with a single dash (-) character between them. All wins and losses are from teams in the same division (the PR ranking ignores games against the FCS division). This is followed by the rankings of each of the prior opponents with a single space between each ranking. You may assume that the number of rankings is always equal to the total games, and that no more than 15 games are played. Use the exact output format demonstrated below where each team is listed in descending order by PR. Round each PR to the nearest hundredth.

<table>
<thead>
<tr>
<th>Sample Input</th>
<th>Output Corresponding to Sample Input</th>
</tr>
</thead>
</table>
| 10
Alabama 7-1 5 77 29 2 92 100 51 33
Auburn 9-0 21 99 67 100 24 63 102 108 51
BoiseState 7-0 101 31 86 2 61 5 35
Nebraska 6-1 3 40 50 80 71 103 106
OhioState 8-1 22 85 53 7 82 43 103 47 4
Oklahoma 7-1 23 96 72 46 71 69 6 45
Oregon 7-0 0 33 52 109 13 49 89
TCU 8-0 86 98 54 21 31 39 72 11
Utah 8-0 69 11 0 5 69 31 21 72
Wisconsin 6-1 11 5 52 104 4 111 5 |
| 1) Auburn 470.56
2) TCU 451.50
3) Oregon 449.29
4) BoiseState 445.86
5) Utah 434.75
6) OhioState 360.67
7) Oklahoma 353.50
8) Nebraska 350.43
9) Alabama 348.63
10) Wisconsin 327.43 |
Theodorus of Cyrene was a Greek mathematician of the 5th century BC. A spiral of right triangles is named after him. This spiral is formed in the following manner.

The spiral is started with an isosceles right triangle, with each leg having a unit length of 1. The end of this first triangle’s hypotenuse is (1,1). Another right triangle is formed, with one leg being the hypotenuse of the prior triangle and the other with length of 1. The process then repeats.

The spiral that Theodorus constructed stopped after the 16th triangle. You are to pick up where he left off. For a given positive integer \( n \), you are interested in the segment whose endpoints are \((0,0)\) and \((a, b)\). This segment is one of the legs of the \( n \)th triangle and the hypotenuse of the \((n-1)\)th triangle. You need to output the ordered pair \((a, b)\).

**Input & Output**
The first line of input contains an integer \( T \), \( 1 \leq T \leq 1000 \), which is the number of test cases. Each test case will consist of a single positive integer \( n \), \( n \leq 10,000,000 \). For each test case, there should be one line of output consisting of the \( x \) and \( y \) coordinates of the end of the \( n \)th hypotenuse. Each coordinate should be rounded to four decimal places and have at least one digit to the left of the decimal place.

**Sample Input**
4
1
2
3
12

**Output Corresponding to Sample Input**
1.0000 0.0000
1.0000 1.0000
0.2929 1.7071
0.3663 -3.4447
Lily is excited about her upcoming birthday party at her home. Lily is very popular and has \( n \) friends. But her house is small, so her parents will only allow her to invite \( m \) friends. Help Lily decide who to invite by listing all possible choices.

**Input**
The first line of input contains an integer \( T, (1 \leq T \leq 1000) \), which is the number of test cases. Each test case contains two integers: \( n \) and \( m \) (in that order) with \( 0 < m \leq n \leq 15 \). The next \( n \) lines contain the first names of Lily’s \( n \) friends. No name contains more than 20 characters. All names in each test case are unique, and consist of only lowercase alphabetic characters.

**Output**
For each test case, print out all the possible ways Lily can choose a set of \( m \) friends to invite to her party. Each set of names should appear on one line, with the names in alphabetical order. In addition, the sets of names should also be in alphabetical order. Number the tests cases (as shown below). Put a blank line after each test case.

**Sample Input**
2  
3 2  
an  
zoe  
janelle  
4 3  
rebecca  
libby  
erin  
nicole  

**Output Corresponding to Sample Input**
Test case 1:  
an janelle  
an zoe  
janelle zoe  

Test case 2:  
erin libby nicole  
erin libby rebecca  
erin nicole rebecca  
libby nicole rebecca
**Problem 5**

**Vigenère’s Cipher**

Vigenère’s Cipher is a polyalphabetic cipher that uses the table below and a sequence of key numbers equal in length to the word being encrypted or decrypted. Unlike simple substitution ciphers like the Caesar’s Cipher, Vigenère’s Cipher hides linguistic patterns and works by taking the key number as the row number and the plaintext letter to be encrypted as the column letter. The intersection of the row number and column letter provides the ciphertext. Close observation will reveal that the letter M is 5 letters after H, and the letter B is 23 letters after E if the alphabet is placed on a circular wheel, etc. Deciphering is done by taking the key number as the row number and finding the ciphertext letter on the row. Once the ciphertext letter is found, the column heading will reveal the plaintext letter.

<table>
<thead>
<tr>
<th>Key</th>
<th>Plaintext</th>
<th>Ciphertext</th>
</tr>
</thead>
<tbody>
<tr>
<td>5</td>
<td>H</td>
<td>M</td>
</tr>
<tr>
<td>23</td>
<td>E</td>
<td>B</td>
</tr>
<tr>
<td>13</td>
<td>L</td>
<td>Y</td>
</tr>
<tr>
<td>2</td>
<td>L</td>
<td>N</td>
</tr>
<tr>
<td>16</td>
<td>O</td>
<td>E</td>
</tr>
</tbody>
</table>

| A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
| 0 | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
| 1 | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A |
| 2 | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B |
| 3 | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C |
| 4 | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D |
| 5 | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E |
| 7 | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G |
| 8 | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |
| 9 | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I |
| 10 | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J |
| 12 | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L |
| 13 | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M |
| 14 | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N |
| 15 | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O |
| 16 | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P |
| 17 | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q |
| 19 | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S |
| 20 | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T |
| 22 | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V |
| 23 | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W |
| 25 | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y |
Input
The input is a sequence of test sets. Each set starts with a line containing a series of cipher key numbers where each number is separated by a space. These key numbers are followed by the letter E for encrypt or letter D for decrypt, followed by a space, and a message comprising only of uppercase and/or lowercase letters. No punctuation or spaces are ever used. The last set consists solely of the string “#” indicating end of input.

Each of the cipher key numbers will be a valid nonnegative integer $n$, $0 \leq n \leq 25$, for each corresponding alphabetic letter that must be either encrypted or decrypted. Assume that the number of key numbers matches the number of letters, and the length of each message is at least one character, but no more than 80 characters.

Output
For each message, output the encrypted or decrypted text message. The case of each letter in the output should match the case of the corresponding letter in the input.

Sample Input
1 E A
1 D A
5 23 13 2 16 E HELLO
5 23 13 2 16 D MBYNE
5 22 10 2 13 20 8 3 E Students
12 4 18 22 D Dsug
13 19 11 4 23 8 15 19 D PattYmae
#

Output Corresponding to Sample Input
B
Z
MBYNE
HELLO
Xpefrhbv
Rock
ChipBell
Problem 6

Medfield GPA Calculator

Medfield College is considering adding the final grades of B+ and C+ to the traditional A, B, C, D, and F grading scale of the college. Under this proposal, a B+ would be worth 3.5 quality points, and a C+ would be worth 2.5 quality points. The other grades would remain the same number of quality points on the 4.0 scale (A = 4.0, B = 3.0, C = 2.0, D = 1.0, F = 0.0).

To compute GPA, multiply the quality points for the grade by the number of credit hours for the course. This produces the quality points for the course. Add the quality points earned for all courses. GPA is equal to the total quality points divided by total credit hours in courses where a grade of A through F is earned. A student’s total earned hours is equal to a sum of all credit hours with a passing grade of D or better. Grades of S or U have no effect on GPA, but a grade of S does contribute to total earned hours. Here’s an example for a student from one semester.

<table>
<thead>
<tr>
<th>Course</th>
<th>Credit Hours * Grade</th>
<th>Quality Points</th>
</tr>
</thead>
<tbody>
<tr>
<td>ENG101</td>
<td>4 * C</td>
<td>8.0</td>
</tr>
<tr>
<td>HIS111</td>
<td>3 * D</td>
<td>3.0</td>
</tr>
<tr>
<td>MAT133</td>
<td>4 * B+</td>
<td>14.0</td>
</tr>
<tr>
<td>CHR150</td>
<td>3 * A</td>
<td>12.0</td>
</tr>
<tr>
<td>PED150</td>
<td>1 * S</td>
<td>0.0</td>
</tr>
</tbody>
</table>

\[ \text{GPA} = \frac{37.0 \text{ Total Quality Points}}{14 \text{ Total Credit Hours}} = 2.64 \text{ with 15 earned hours} \]

Input & Output
The first line of input contains an integer \( T \), (1 \( \leq \) \( T \) \( \leq \) 1000), the number of student records. This is followed by \( T \) student records. Each student record consists of one line with student name (one string with no spaces in format LastName,First), a single space, and number of courses \( n \), (1 \( \leq \) \( n \) \( \leq \) 10), taken for the term. This is followed by \( n \) course reports. Each course report is made up of a course name (one string with no spaces), a single space, the final grade (either A, B+, B, C+, C, D, F, S, or U), a single space, and number of credit hours for the course. Use the exact output format below for the student, their earned hours, and final term GPA.

**Sample Input**
5
Lightyear,Buzz 4
HIS111 A 3
CSC204 B+ 4
SPN111 C 4
ENG108 B 3
Head,MrPotato 4
CSC204 C 4
SPN111 B 4
MUS151 C+ 3
PED151 U 1
Peep,Bo 3
CSC204 B+ 4
SPN111 A 4
MAT191 C 4
Dog,Slinky 3
PHY161 D 4
MAT191 C+ 4
PRE111 F 4
Doll,Barbie 3
HIS111 A 3
PHY105 A 5
MAT191 A 4

**Output Corresponding to Sample Input**
Lightyear,Buzz has earned 14 hours with a GPA of 3.07
Head,MrPotato has earned 11 hours with a GPA of 2.50
Peep,Bo has earned 12 hours with a GPA of 3.17
Dog,Slinky has earned 8 hours with a GPA of 1.17
Doll,Barbie has earned 12 hours with a GPA of 4.00
Problem 7

Australian Word Search

Andy is flipping through his Delta Sky Magazine on the long fifteen hour flight from Los Angeles to Sydney, and comes across a fun word search game. It is filled with lots of Australian lingo he would love to learn before arrival. It also makes him think a lot about how a computer might go about finding words in the grid.

Your job is to write a computer program that searches for words in the game. Words can be found horizontally or vertically in a 10 by 10 grid of characters, as well as along either of the two main diagonals that cross through the center of the grid. (The center of the grid has coordinates (4,4) where the first letter in the upper-left-hand corner has coordinates (0,0).)

Words can be found in any direction (left to right, right to left, up and down vertically, or moving either way along the two main diagonals). Each word is unique, and will be found only once in a given direction. All words are at least two characters long, and no more than ten.

Input
The input will start with ten lines each filled with exactly ten uppercase alphabetic characters, and no spaces. This is followed by the integer \( T \), \( (1 \leq T \leq 1000) \), which is the number of words we are searching for within the grid. This is followed by \( T \) lines each containing a single word at the start. Each word will consist of all uppercase alphabetic characters, and no spaces.

Output
Your output will consist of \( T \) lines in the format below. Report back whether each word was found horizontally, vertically, diagonally, or not found at all in the format demonstrated below.

<table>
<thead>
<tr>
<th>Sample Input</th>
<th>Output Corresponding to Sample Input</th>
</tr>
</thead>
<tbody>
<tr>
<td>RGNAREMOOB</td>
<td>BOOMERANG was found horizontally.</td>
</tr>
<tr>
<td>BEMQASAEAR</td>
<td>OZ was found vertically.</td>
</tr>
<tr>
<td>ZXESTSTIYO</td>
<td>REEF was found diagonally.</td>
</tr>
<tr>
<td>OLMFEYEUAG</td>
<td>MATE was found vertically.</td>
</tr>
<tr>
<td>GLDINGOESI</td>
<td>HOON was found diagonally.</td>
</tr>
<tr>
<td>IAKANOAROO</td>
<td>DINGOES was found horizontally.</td>
</tr>
<tr>
<td>NRYAKKORDD</td>
<td>JACKAROO was not found.</td>
</tr>
<tr>
<td>EOPZREEHLL</td>
<td></td>
</tr>
<tr>
<td>KOALAUHOSN</td>
<td></td>
</tr>
<tr>
<td>EIOUAEIOUP</td>
<td></td>
</tr>
<tr>
<td>7</td>
<td></td>
</tr>
<tr>
<td>BOOMERANG</td>
<td></td>
</tr>
<tr>
<td>OZ</td>
<td></td>
</tr>
<tr>
<td>REEF</td>
<td></td>
</tr>
<tr>
<td>MATE</td>
<td></td>
</tr>
<tr>
<td>HOON</td>
<td></td>
</tr>
<tr>
<td>DINGOES</td>
<td></td>
</tr>
<tr>
<td>JACKAROO</td>
<td></td>
</tr>
</tbody>
</table>
Problem 8
Windows

April is not very tidy with the desktop of her computer. She has the habit of opening windows on the screen, and then forgetting to close the application that created them. The result, of course, is a very cluttered desktop with some windows just peeking out from behind others and some completely hidden. Given that April doesn’t log off for days, this is a formidable mess. Your job is to determine which window (if any) gets selected when April clicks on a certain position of the screen.

April’s screen has a resolution of 10^6 by 10^6. When each window opens its position is given by the upper-left-hand corner, its width, and its height. (Assume position (0,0) is the location of the pixel in the upper-left-hand corner of her desktop. So, the lower-right-hand pixel has location (999999, 999999).)

Input
Input for each test case is a sequence of desktop descriptions. Each description consists of a line containing a positive integer n, the number of windows, followed by n lines, n ≤ 100, describing windows in the order in which April opened them, followed by a line containing a positive integer m, the number of queries, followed by m lines, each describing a query. Each of the n window description lines contains four integers r, c, w, and h, where (r, c) is the row and column of the upper left pixel of the window, 0 ≤ r, c ≤ 999,999, and w and h are the width and height of the window, in pixels, 1 ≤ w, h.

All windows will lie entirely on the desktop (i.e., no cropping). Each of the m query description lines contains two integers cr and cc, the row and column number of the location (which will be on the desktop). The last test case is followed by a line containing 0.

Output
Using the format shown, print the desktop number, beginning with 1, followed by m lines, one per query. The i-th line should say either “window k”, where k is the number of the window clicked on, or “background” if the query hit none of the windows. We assume that windows are numbered consecutively in the order in which April opened them, beginning with 1. Note that querying a window does not bring that window to the foreground on the screen.
Sample Input
3
1 2 3 3
2 3 2 2
3 4 2 2
4
3 5
1 2
4 2
3 3
2
5 10 2 10
100 100 100 100
2
5 13
100 101
0

Output Corresponding to Sample Input
Desktop 1:
window 3
window 1
background
window 2
Desktop 2:
background
window 2